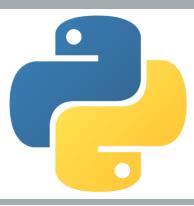
PYTHON BOOT CAMP

<u>Module 3:</u> <u>Math Functions, Strings,</u> <u>and Objects</u>



Objectives

- To solve mathematics problems by using the functions in the math module (§3.2).
- To represent and process strings and characters (§§3.3-3.4).
- To encode characters using ASCII and Unicode (§§3.3.1-3.3.2).
- To use the ord to obtain a numerical code for a character and chr to convert a numerical code to a character (§3.3.3).
- To represent special characters using the escape sequence (§3.3.4).
- To invoke the print function with the end argument (§3.3.5).
- To convert numbers to a string using the **str** function (§3.3.6).
- To use the + operator to concatenate strings (§3.3.7).
- To read strings from the console (§3.3.8).
- To introduce objects and methods (§3.5).
- To format numbers and strings using the format function (§3.6).
- To draw various shapes (§3.7).
- To draw graphics with colors and fonts (§3.8).

First, what is a function?

- A function is a group of statements that performs a specific task
- And we can broadly classify functions into:
 - 1. Those functions that we will fully define, write, and customize
 - This comes later (Chapter 6)
 - 2. Those functions that are prebuilt and available to the programmer as part of the library of the given language
- Guess what?
 - We've been using functions since Day 1!
 - eval, input, int, and even print
 - These are all built-in functions and part of the Python library

Some built-in math functions:

TABLE 3.1 Simple Python Built-in Functions		
Function	Description	Example
abs(x)	Returns the absolute value for x.	abs(-2) is 2
max(x1, x2,)	Returns the largest among x1, x2,	max(1, 5, 2) is 5
min(x1, x2,)	Returns the smallest among x1, x2,	min(1, 5, 2) is 1
pow(a, b)	Returns a^b . Same as a ** b .	pow(2, 3) is 8
round(x)	Returns an integer nearest to x . If x is equally close to two integers, the even one is returned.	round(5.4) is 5
		round(5.5) is 6
		round(4.5) is 4
round(x, n)	Returns the float value rounded to n digits after the decimal point.	round(5.466, 2) is 5.47
		round(5.463, 2) is 5.46

These functions are so common that no "imports" are needed in order for them to work...you just use them

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Module 3: Math Functions, Strings, & Objects

Some built-in math functions:

```
>>> abs(-3) # Returns the absolute value
>>> abs(-3.5) # Returns the absolute value
3.5
>>> max(2, 3, 4, 6) # Returns the maximum number
6
>>> min(2, 3, 4) # Returns the minimum number
>>> pow(2, 3) # Same as 2 ** 3
8
>>> pow(2.5, 3.5) # Same as 2.5 ** 3.5
24.705294220065465
>>> round(3.51) # Rounds to its nearest integer
4
>>> round(3.4) # Rounds to its nearest integer
3
>>> round(3.1456, 3) # Rounds to 3 digits after the decimal point
3.146
>>>
```

Additional math functions:

- The Python math module can be imported and provides additional math functions and some famous constants
 - Functions include:
 - exp, sqrt, log, sin, cos, and more
 - Constants include:
 - **PI** and **e**
 - You import the module similar to importing turtle
 - You simply type:
 - import math
 - at the beginning of your program

Function	Description	Example
fabs(x)	Returns the absolute value for \mathbf{x} as a float.	fabs(-2) is 2.0
ceil(x)	Rounds \mathbf{x} up to its nearest integer and returns that integer.	ceil(2.1) is 3 ceil(-2.1) is -2
floor(x)	Rounds x down to its nearest integer and returns that integer.	floor(2.1) is 2 floor(-2.1) is -3
exp(x)	Returns the exponential function of $x (e^x)$.	exp(1) is 2.71828
log(x)	Returns the natural logarithm of x.	log(2.71828) is 1.0
log(x, base)	Returns the logarithm of \mathbf{x} for the specified base.	log(100, 10) is 2.0
sqrt(x)	Returns the square root of x .	sqrt(4.0) is 2
sin(x)	Returns the sine of x. x represents an angle in radians.	sin(3.14159 / 2) is 1 sin(3.14159) is 0
asin(x)	Returns the angle in radians for the inverse of sine.	asin(1.0) is 1.57 asin(0.5) is 0.523599
cos(x)	Returns the cosine of \mathbf{x} . \mathbf{x} represents an angle in radians.	cos(3.14159 / 2) is 0 cos(3.14159) is -1
acos(x)	Returns the angle in radians for the inverse of cosine.	acos(1.0) is 0 acos(0.5) is 1.0472
tan(x)	Returns the tangent of \mathbf{x} . \mathbf{x} represents an angle in radians.	tan(3.14159 / 4) is 1 tan(0.0) is 0
degrees(x)	Converts angle x from radians to degrees.	degrees(1.57) is 90
radians(x)	Converts angle \mathbf{x} from degrees to radians.	radians(90) is 1.57

Module 3: Math Functions, Strings, & Objects

Example program:

LISTING 3.1 MathFunctions.py

import math # import math module to use the math functions 1 2

```
3
  # Test algebraic functions
```

```
4 print("exp(1.0) =", math.exp(1))
```

```
print("log(2.78) =", math.log(math.e))
5
```

```
print("log10(10, 10) =", math.log(10, 10))
6
```

```
print("sqrt(4.0) =", math.sqrt(4.0))
7
```

```
8
9
  # Test trigonometric functions
```

```
10 print("sin(PI / 2) =", math.sin(math.pi / 2))
```

```
11 print("cos(PI / 2) =", math.cos(math.pi / 2))
12 print("tan(PI / 2) =", math.tan(math.pi / 2))
```

```
13 print("degrees(1.57) =", math.degrees(1.57))
```

```
14 print("radians(90) =", math.radians(90))
```

```
\exp(1.0) = 2.71828182846
log(2.78) = 1.0
\log 10(10, 10) = 1.0
sqrt(4.0) = 2.0
sin(PI / 2) = 1.0
\cos(PI / 2) = 6.12323399574e-17
tan(PI / 2) = 1.63312393532e+16
degrees(1.57) = 89.9543738355
radians(90) = 1.57079632679
```

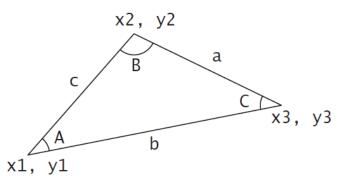
Module 3: Math Functions, Strings, & Objects

Example usage:

- Having access to these math functions opens doors to solve a variety of computational problems
- An important note:
 - Many are not comfortable with math
 - But that's no reason to be scared when seeing formulas!
 - You needn't derive the formula
 - All we need to know is what the formula does and how to use it
 - Just like we didn't "derive" how a car engine was put together
 - We just need to know what it does and how to use it

Example usage:

For example, given three vertices of a triangle:



we can compute the three angles as follows:

$$A = acos((a * a - b * b - c * c) / (-2 * b * c))$$

$$B = acos((b * b - a * a - c * c) / (-2 * a * c))$$

$$C = acos((c * c - b * b - a * a) / (-2 * a * b))$$

• And with that knowledge, we can write a simple program...

Example usage:

```
LISTING 3.2 ComputeAngles.py
   import math
1
2
3
  x1, y1, x2, y2, x3, y3 = eval(input("Enter three points: "))
 4
5 a = math.sqrt((x_2 - x_3) * (x_2 - x_3) + (y_2 - y_3) * (y_2 - y_3))
6 b = math.sqrt((x1 - x3) * (x1 - x3) + (y1 - y3) * (y1 - y3))
   c = math.sqrt((x1 - x2) * (x1 - x2) + (y1 - y2) * (y1 - y2))
7
8
9 A = math.degrees(math.acos((a * a - b * b - c * c) / (-2 * b * c)))
10 B = math.degrees(math.acos((b * b - a * a - c * c) / (-2 * a * c)))
   C = math.degrees(math.acos((c * c - b * b - a * a) / (-2 * a * b)))
11
12
   print("The three angles are ", round(A * 100) / 100.0,
13
        round(B * 100) / 100.0, round(C * 100) / 100.0)
14
```

Enter three points: 1, 1, 6.5, 1, 6.5, 2.5 The three angles are 15.26 90.0 74.74

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Module 3: Math Functions, Strings, & Objects

Check Point:

Evaluate the following functions:

- (a) math.sqrt(4)
- (b) math.sin(2 * math.pi)
- (c) math.cos(2 * math.pi)
- (d) min(2, 2, 1)
- (e) math.log(math.e)
- (f) math.exp(1)
- $(g) \max(2, 3, 4)$
- (h) abs(-2.5)
- (i) math.ceil(-2.5)

- (j) math.floor(-2.5)
- (k) round(3.5)
- (l) round(-2.5)
- (m) math.fabs(2.5)
- (n) math.ceil(2.5)
- (o) math.floor(2.5)
- (p) round(-2.5)
- (q) round(2.6)
- (r) round(math.fabs(-2.5))

What is a string?

- A string is a sequence of characters
 - And this sequence could just be a string of numbers
 - Example:
 - "3.145" would be considered a string with five characters in it
- In Python, a string must be enclosed in either double quotes (") or single quotes (')

Examples:

```
message = "good morning"
letter = "A"
letter = 'A' # these are the same!
number_string = "2018" # same as number_string = '2018'
```

What is a string?

- Note:
 - Python does not have a specific data type for a single character
 - Many (most) languages do!
 - In Python, a single character is simply represented as a singlecharacter string
- We'd like to be consistent with other languages:
- Therefore:
 - Double quotes will be used for a string with more than one character
 - Single quotes will be used for a single character string

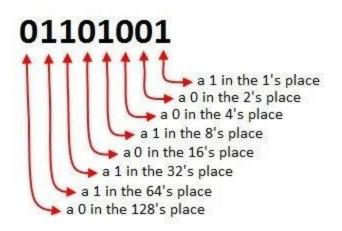
A (very quick) primer on numbers!

- The most common number system and the one we use most often is decimal
- Decimal is base what?
 - Base 10
- What does this mean?
 - Means there are ten numbers we use
 - 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9
- Computers use binary numbers. Binary is base what?
 - Base 2
- What does this mean?
 - There are only two numbers used: 0 and 1 (known as bits)

- A (very quick) primer on numbers!
 - How to convert from binary to decimal?
 - This is actually really easy
 - Each digit in a binary number can be 1 or 0
 - Think of this as on or off
 - And each of these digits has a value (a weight)
 - And that value counts towards the total if the bit is set to 1 (if it is "on")
 - The least-significant bit is on the right
 - If the bit is 1, it's value is simply 1
 - The values of each digit to the left increase by powers of 2
 - **2**, 4, 8, 16, 32, 64, 128, 256, ...
 - This is easiest to understand with pictures and examples...

A (very quick) primer on numbers!

Consider the following:

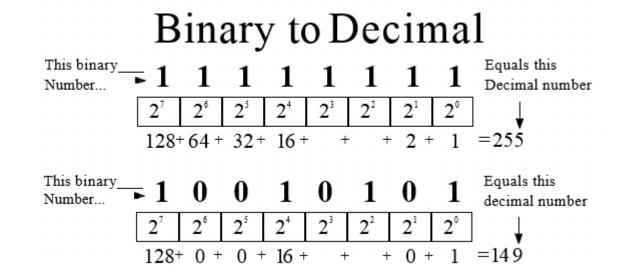


• The decimal equivalent is:

64 + 32 + 8 + 1 = 105

A (very quick) primer on numbers!

Another example/picture:



A (very quick) primer on numbers!

Check Yourself:

What is the decimal value of the following:

- **1001**
 - 9
- **1010**
 - **1**0
- 0111
 - 7
- **1111**
 - **1**5
- **1000**

- 8

- A (very quick) primer on numbers!
 - Binary is easy to understand (once we practice it)
 - But it's a pain to represent!
 - It takes so much digits to represent a basic number!
 - Hexadecimal to the rescue!
 - Hexadecimal (aka Hex) is another number system
 - Hex is base what?
 - Hex is base 16
 - What does this mean?
 - It means there are 16 numbers
 - Huh? But we only have 10 numbers (0 to 9). How do we get 16???
 - It is kinda weird at first, but here are the 16 hex numbers:
 - 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F
 - So F in hex is the same as 15 in decimal

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Module 3: Math Functions, Strings, & Objects

A (very quick) primer on numbers!

So why hex?

Hex can very seamlessly (easily) represent binary numbers

Decimal (Base 10)	Binary (Base 2)	Hexadecimal (Base 16)
0	0000	0
1	0001	1
2	0010	2
3	0011	3
4	0100	4
5	0101	5
6	0110	6
7	0111	7
8	1000	8
9	1001	9
10	1010	А
11	1011	В
12	1100	С
13	1101	D
14	1110	E
15	1111	F

Module 3: Math Functions, Strings, & Objects

Character encoding:

- Computer uses binary numbers internally
 - a sequence of 0s and 1s
- All characters are in fact stored as a sequence of 0s and 1s
- Mapping a character to its binary representation is called character encoding
- There are different ways to map a character to binary
- Two popular varieties:
 - ASCII
 - Unicode

ASCII

Stands for:

American Standard Code for Information Interchange

- no need to remember that!
- ASCII is a 7-bit encoding scheme
 - What does that mean?
 - This means that a total of 7 bits are used to represent characters
 - Example:
 - 0110110 is a group of 7 bits
 - It represents a specific character in ASCII
 - 1100100 is another group of 7 bits
 - And it represents a different character in ASCII
 - With 7 bits, this means 2⁷ possible different groups of those bits
 - So 128 different characters can be encoded with ASCII

ASCII

- 128 characters is not very much
 - Sure, it may suffice a single language, but not much more
 - Consider 26 uppercase characters in English alphabet
 - And 26 lower case
 - Yes, these are encoded differently...they are different characters
 - That's already 52 characters
 - Now add in numbers, punctuation marks, and other common characters
 - We quickly use up those 128 spots in ASCII
- Long story short:
 - ASCII simply isn't enough
 - So enter Unicode...

Unicode

- Easy summary:
 - Allows encoding of 1,114,112 characters!
 - Yes, MORE than sufficient for everything we need

Encoding:

- Unicode starts with \u and then has 4 hexadecimal digits
- These digits run from \u0000 to \uFFFF

Example:



7∕∉ Pyth	on Turtle Graphics	
	欢迎 α β γ	
		<u>+</u>

ord and chr functions:

- Python provides two helpful functions:
 - ord (ch) function for returning the ASCII code for the character
 ch
 - chr (code) function for returning the character represented by the code.

```
>>> ch = 'a'
>>> ord(ch)
97
>>> chr(98)
'b'
>>> ord('A')
65
>>>
```

Escape Sequences for Special Characters

- Consider the following example:
 - How would you print a message with quotation marks in Python?
 - Meaning, what if you wanted to quote someone and print the actual quotation
 - Could you do this?

print("He said, "John's program is easy to read"")

- The answer is no. That won't work
- When Python sees the second double quotation mark, it understands that the string is finished/complete
- You would print this as follows:
 - print("He said, \"John's program is easy to read\"")
- Notice the backslashes...that is called an <u>ESCAPE sequence</u>

- Escape Sequences for Special Characters
 - Escape sequences is a special notation used to represent special characters
 - This notation consists of a backslash followed by a letter or a combination of digits

TABLE 3.3 Python Escape Se	quences	
Character Escape Sequence	Name	Numeric Value
\b	Backspace	8
\t	Tab	9
\n	Linefeed	10
\ f	Formfeed	12
\r	Carriage Return	13
VV	Backslash	92
Λ'	Single Quote	39
Λ"	Double Quote	34

Printing without the newline

- The print function automatically prints a new line (\n)
 - This causes the output to advance to the next line
- What if you don't want to advance to the next line?
 - You use the print function with a special argument print(item, end = "anyendingstring")
- For example, consider the following code:

print("AAA", end = ' ')
print("BBB", end = '')
print("CCC", end = '***')
print("DDD", end = '***')

Output: AAA BBBCCC***DDD***

Printing without the newline

Another example:

Consider the following code:

```
radius = 3
print("The area is", radius * radius * math.pi, end = ' ')
print("and the perimeter is", 2 * radius)
```

• The output:

The area is 28.26 and the perimeter is 6

The str function

The str function can be used to convert a number into a string

```
>>> s = str(3.4) # Convert a float to string
>>> s
'3.4'
>>> s = str(3) # Convert an integer to string
>>> s
'3'
>>>
```

- The String Concatenation Operator
 - We normally view the + sign as addition
 - and this is okay
 - But in programming languages, the + operator has another meaning: concatenation
 - We can use the + operator to concatenate two strings

```
1 >>> message = "Welcome " + "to " + "Python"
2 >>> message
3 'Welcome to Python'
4 >>> chapterNo = 3
5 >>> s = "Chapter " + str(chapterNo)
6 >>> s
7 'Chapter 3'
8 >>>
```

Reading strings from the console

- We've actually been doing this for some time now
- Python understands all input as a string
 - We then used the eval and int functions to convert the string to other values
- Example:

```
Dle: s1 = input("Enter a string: ")
s2 = input("Enter a string: ")
s3 = input("Enter a string: ")
print("s1 is " + s1)
print("s2 is " + s2)
print("s3 is " + s3)
```

Enter a string: Welcome
Enter a string: to Finter
Enter a string: Python - Enter
s1 is Welcome
s2 is to
s3 is Python

Module 3: Math Functions, Strings, & Objects

Problem 1: Range Calculator

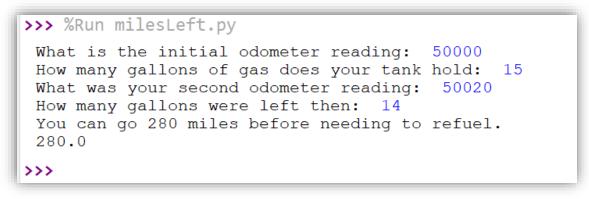
- Write a program to calculate the number of miles remaining before you run out of gas!
 - This is very common in most cars these days.

Remember:

- Step 1: Problem-solving Phase
- Step 2: Implementation Phase

Problem 1: Range Calculator

- Write a program to calculate the number of miles remaining before you run out of gas!
 - This is very common in most cars these days.
- Step 1: Problem-solving Phase
 - First, let us see a sample run of the program...



Problem 1: Range Calculator

- Write a program to calculate the number of miles remaining before you run out of gas!
 - This is very common in most cars these days.
- Step 1: Problem-solving Phase
 - After some thought (few minutes probably)...
 - Hopefully we realize the following:
 - We need the miles driven
 - Ending reading starting reading
 - We need the amount of gas used
 - Starting gas ending gas
 - We need to calculate the miles per gallon thus far
 - And we then multiply that times the gas remaining...

Problem 1: Range Calculator

- Write a program to calculate the number of miles remaining before you run out of gas!
 - This is very common in most cars these days.
- Step 2: Implementation Phase
 - Check portal for a sample solution!

What are objects and OOP?

- OOP stands for Object-oriented Programming
 - For now...that's all you need to know!
 - We'll get to that concept later on
- At the core of OOP is objects...so what are objects?
- Well, in Python, ALL data are objects!
 - This includes numbers and strings
 - And this is different from many other languages

What are objects and OOP?

- "Um...again, so what are objects?!?"
 - Consider and int variable such as a = 777
 - normally students would imagine that int value, 777, just floating around in computer memory
 - With objects, we do not think of variable a as storing the value 777
 - Rather, a stores a reference, and that reference points to a box
 - and the value 777 can be found inside that box
- A picture is helpful
 - Given the code:
 - a = 777

a

Here's how you can visualize this:

777

What are objects and OOP?

- "So why is this helpful?"
 - Long answer: many reasons...and they will come up
 - But for now, we can perform operations on these objects!
 - Operations made for and used with objects are called methods.

Example:

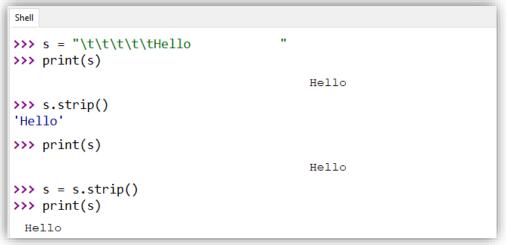
- s = "Welcome"
 - Remember: the variable s stores a reference that points to a box, and the string "Welcome" can be found inside that box
 - Now we can perform methods on that box!

```
s1 = s.lower()
print(s1) # "welcome" is printed
s2 = s.upper()
print(s2) # "WELCOME" is printed
```

- Some interesting functions for objects
 - Python gives the id and the type functions to get information about our objects
 - id: this is the actual reference saved inside the variable
 - Such as the reference saved in "a" on that last picture
 - type: this refers to the type
 of the given object
 - These functions are rarely used in programming
 - But they are helpful when first learning about objects

Shell	
>>> a = 777 >>> id(a) 92839968	
<pre>>>> type(a) <class 'int'=""></class></pre>	
>>> b = 3.0 >>> id(b) 92396256	
<pre>>>> type(b) <class 'float'=""></class></pre>	
<pre>>>> s = "Welcome" >>> id(s) 92835968</pre>	
<pre>>>> type(s) <class 'str'=""></class></pre>	

- Additional useful String methods
 - strip():
 - used to removed whitespace characters from both sides of a string
 - Whitespace includes spaces, tabs, and newlines



- You can read about other methods here:
 - <u>https://www.w3schools.com/python/python_ref_string.asp</u>

Module 3: Math Functions, Strings, & Objects

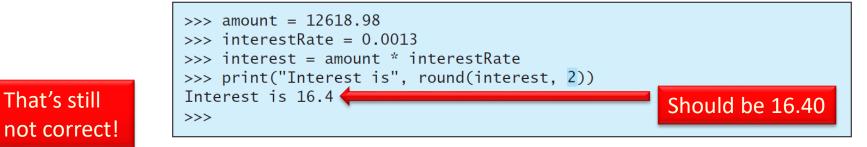
Formatting is often helpful and even needed

Consider the following code:

```
>>> amount = 12618.98
>>> interestRate = 0.0013
>>> interest = amount * interestRate
>>> print("Interest is", interest)
Interest is 16.404674
>>>
```

- The interest is currency
 - So it's desirable to have two decimals

We could rewrite the code as follows



Formatting is often helpful and even needed

The solution is formatted printing:

```
>>> amount = 12618.98
>>> interestRate = 0.0013
>>> interest = amount * interestRate
>>> print("Interest is", format(interest, ".2f"))
Interest is 16.40
>>>
```

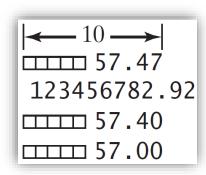
Syntax:

format(item, format-specifier)

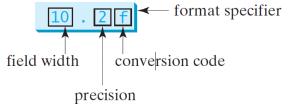
- Here, item is a number of a string
- And format-specifier is a string that specifies how the item is to be formatted

- Formatting Floating-Point Numbers
 - Consider the following code and output:

```
print(format(57.467657, "10.2f"))
print(format(12345678.923, "10.2f"))
print(format(57.4, "10.2f"))
print(format(57, "10.2f"))
```



- You specify a width, a precision, and a conversion code
 - The width is how many spaces to print the number
 - The precision is how many digits after the decimal place
 - The conversion code, in this example, f, tells Python that we are formatting a floating-point number



Formatting Floating-Point Numbers

Comments:

- By default, the number is aligned to the right within the specified width
- If the number is larger than the width, the width is automatically increased
- You can also omit the width specifier
 - Example: print(format(57.467657, ".2f"))
 - In this case, the width is set automatically

Formatting as a Percentage

- We can use conversion code % to format a percentage
 - And if we use "10.2%" as the full format specifier, the number is first multiplied by 100 and displayed with a % sign

print(format(0.53457, "10.2%"))
print(format(0.0033923, "10.2%"))
print(format(7.4, "10.2%"))
print(format(57, "10.2%"))

Result:

 ↓
 10 →

 □□□□ 53.46%

 □□□□ 0.34%

 □□□ 740.00%

 □□ 5700.00%

Justifying Format

Default: number is right justified

We can use the < or > symbols for justification as well

```
print(format(57.467657, "10.2f"))
print(format(57.467657, "<10.2f"))</pre>
```

displays

| ← 10 → | □ □ □ 57.47 57.47

Formatting Integers

- The conversion codes d, x, o, and b:
 - used to format an integer in decimal, hexadecimal, octal, or binary
 - We can also specify a width for the conversion

```
print(format(59832, "10d"))
print(format(59832, "<10d"))
print(format(59832, "10x"))
print(format(59832, "<10x"))</pre>
```

displays

```
| ← 10 → |
□ □ □ 59832
59832
□ □ □ 0 e9b8
e9b8
```

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Module 3: Math Functions, Strings, & Objects

Formatting Strings

You can use the conversion code s to format a string with a specified width

print(format("Welcome to Python", "20s"))
print(format("Welcome to Python", "<20s"))
print(format("Welcome to Python", ">20s"))
print(format("Welcome to Python and Java", ">20s"))

displays

Frequently Used Specifiers

Specifier	Format
"10.2f"	Format the float item with width 10 and precision 2.
"10.2e"	Format the float item in scientific notation with width 10 and precision 2.
"5d"	Format the integer item in decimal with width 5.
"5x"	Format the integer item in hexadecimal with width 5.
"5o"	Format the integer item in octal with width 5.
"5b"	Format the integer item in binary with width 5.
"10.2%"	Format the number in decimal.
"50s"	Format the string item with width 50.
"<10.2f"	Left-justify the formatted item.
">10.2f"	Right-justify the formatted item.

- Write a program to determine the number of cups of Kool-Aid that must be sold in order to meet a specified goal (see sample).
- Remember:
 - Step 1: Problem-solving Phase
 - Step 2: Implementation Phase

- Write a program to determine the number of cups of Kool-Aid that must be sold in order to meet a specified goal (see sample).
- Step 1: Problem-solving Phase
 - First, let us see a sample run of the program...

```
>>> %Run koolaid.py
How many dollars is the rent for your stand? 5
How many cents do the materials cost, per glass? 2
How many cents do you charge per glass? 25
What is your profit goal, in dollars? 50
You must sell 240 cups of Kool-Aid to meet your goal.
>>>
```

- Write a program to determine the number of cups of Kool-Aid that must be sold in order to meet a specified goal (see sample).
- Step 1: Problem-solving Phase
 - Spend some time to think this one through on paper
 - Once you have it solved on paper, try to code it
 - You'll likely get really close
 - and maybe exactly close on some cases
 - But there's one additional thing to think of...

- Write a program to determine the number of cups of Kool-Aid that must be sold in order to meet a specified goal (see sample).
- Step 2: Implementation Phase
 - Check portal for a sample solution!

PYTHON BOOT CAMP

<u>Module 3:</u> <u>Math Functions, Strings,</u> <u>and Objects</u>

